



Synchromodality in the Physical Internet

Real-time Switching in a Multimodal Network with Stochastic Transit Times

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A deep decarbonization of the logistics industry is needed.

- Enormous amount of CO₂ emissions from the freight transportation sector
- Modal shift towards less carbon-intensive transportation modes



- **The Physical Internet**
Connect logistics networks into an integrated network

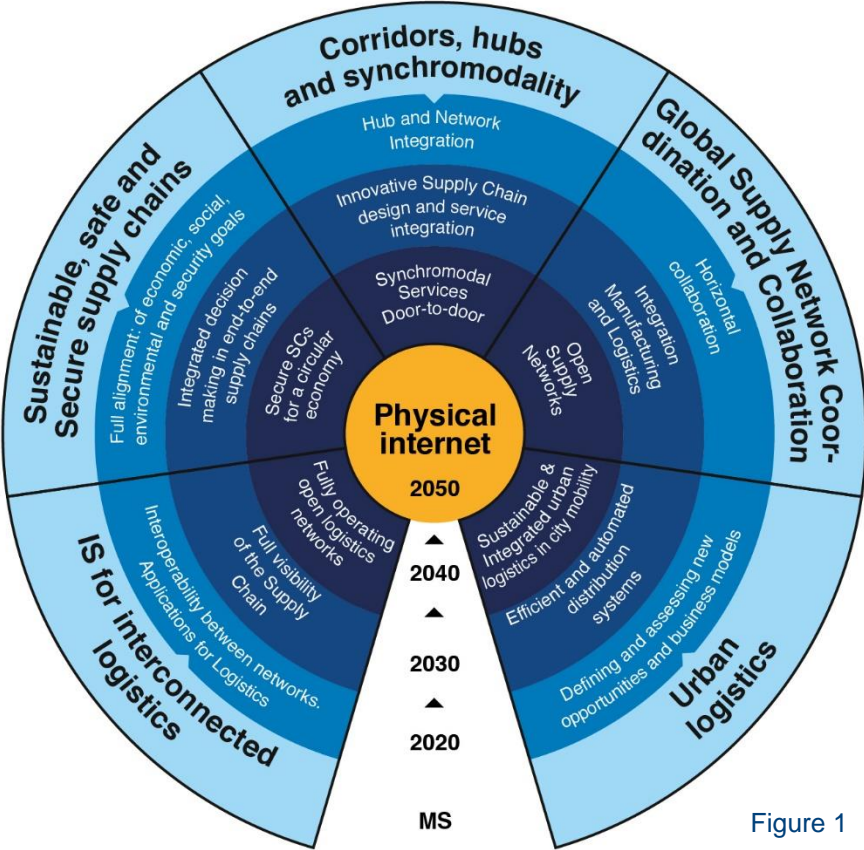


Figure 1. Adapted from *Roadmap: Corridors, Hubs and Synchronomodality*, by ETP-Alice. Retrieved from [http:// etp- logistics.eu](http://etp-logistics.eu).

Figure 1

Synchromodality offers a solution to reduce emissions.

- Enormous amount of CO₂ emissions from the freight transportation sector
- Modal shift towards less carbon-intensive transportation modes



- The Physical Internet ➤ Synchromodality
Connect logistics networks into an integrated network

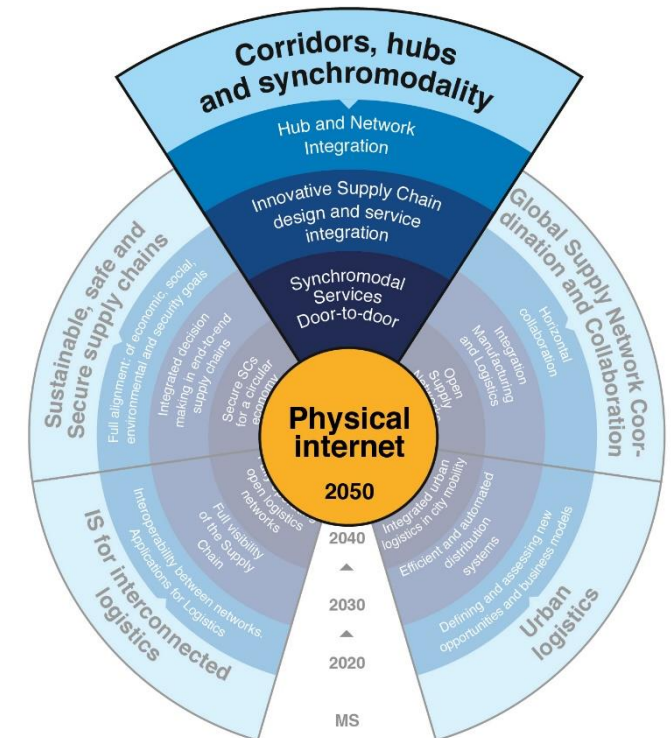


Figure 1. Adapted from *Roadmap: Corridors, Hubs and Synchromodality*, by ETP-Alice. Retrieved from [http:// etp- logistics.eu](http://etp-logistics.eu).

Figure 1

Synchromodality - Towards the Physical Internet.

- Multiple transportation modes



- Real-time information



- Select the best transportation mode at all times
- Use modalities more efficiently and exploit all advantages

Synchromodality efficiently copes with uncertainty in transit times.

Synchromodality in a network with **stochastic transit times**

- Unreliability in transportation system
- Optimal transportation decision given the transit time outcome



Synchromodality efficiently copes with uncertainty in transit times.

Synchromodality in a network with **stochastic transit times**

- Unreliability in transportation system
- Optimal transportation decision given the transit time outcome



Research objective

- Develop synchromodal planning model to construct optimal transportation routes
- Insights in the advantages of synchromodality



Cost



Service quality



Sustainability

Synchromodality efficiently copes with uncertainty in transit times.

Synchromodality in a network with **stochastic transit times**

- Unreliability in transportation system
- Optimal transportation decision given the transit time outcome



Research objective

- Develop synchromodal planning **model** to construct optimal transportation routes
- **Insights** in the advantages of synchromodality



Cost

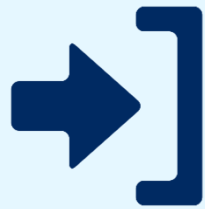


Service quality



Sustainability

Our model constructs optimal transportation routes given the stochastic transit times.



Input

- Multimodal network
- Set of orders



Optimization model

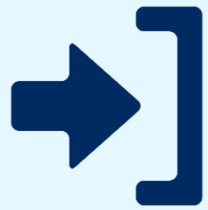
- Construct optimal transportation routes
- MILP



Output

- Decision guide conditional on transit time outcome

Input of the model



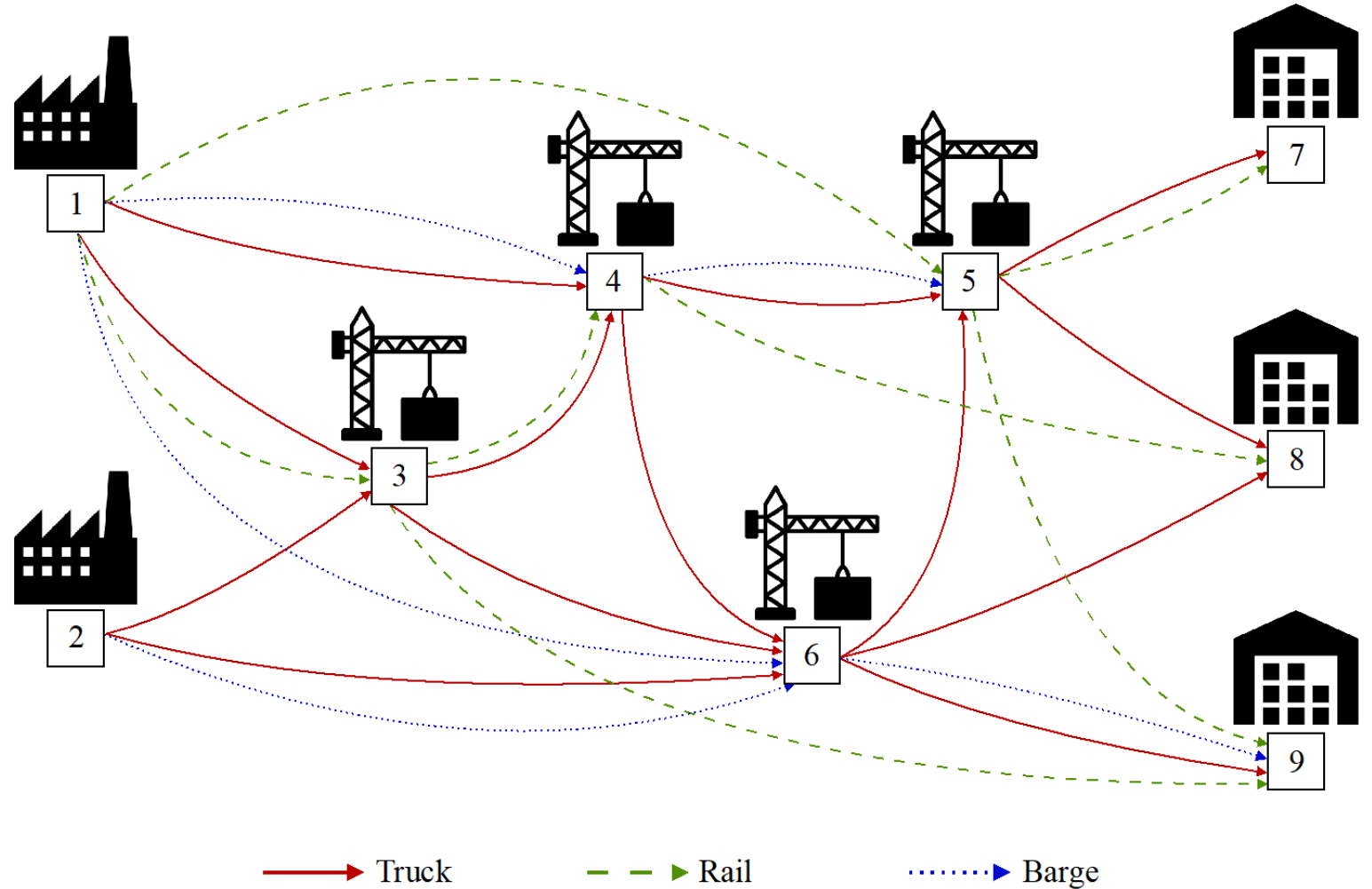
Input

- Multimodal network
- Set of orders
- Input parameters

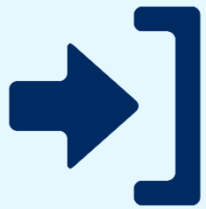
Origin terminals

Intermediate terminals

Destination terminals

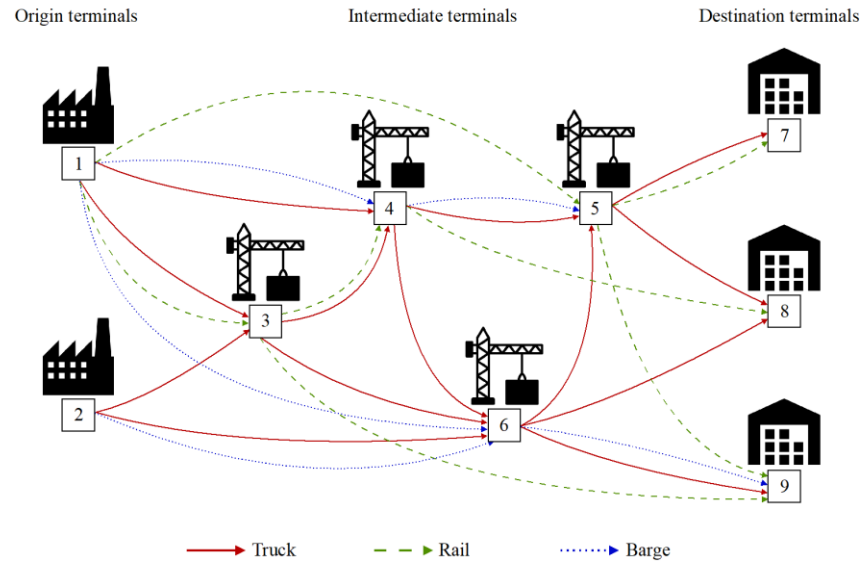


Input of the model: stochasticity is modeled through scenarios.



Input

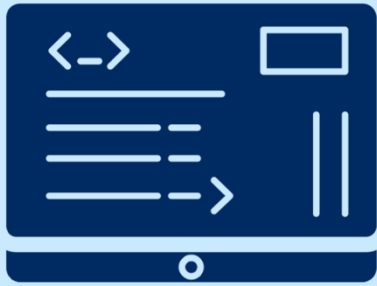
- Multimodal network
- Set of orders
- Input parameters



Transit time stochasticity

- Transit time scenarios
- Probability distribution

The optimization model is formulated as a mixed-integer linear programming problem.



Optimization model

- Construct optimal transportation routes
- MILP

- Construct optimal transportation routes
 - Routing decisions
 - Stochasticity: adapt routes to real-time information

- Mixed-integer linear programming problem

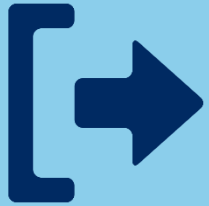
Minimize

- Leg transportation cost
- Terminal transshipment cost
- Overdue penalty cost

Low cost

On-time delivery

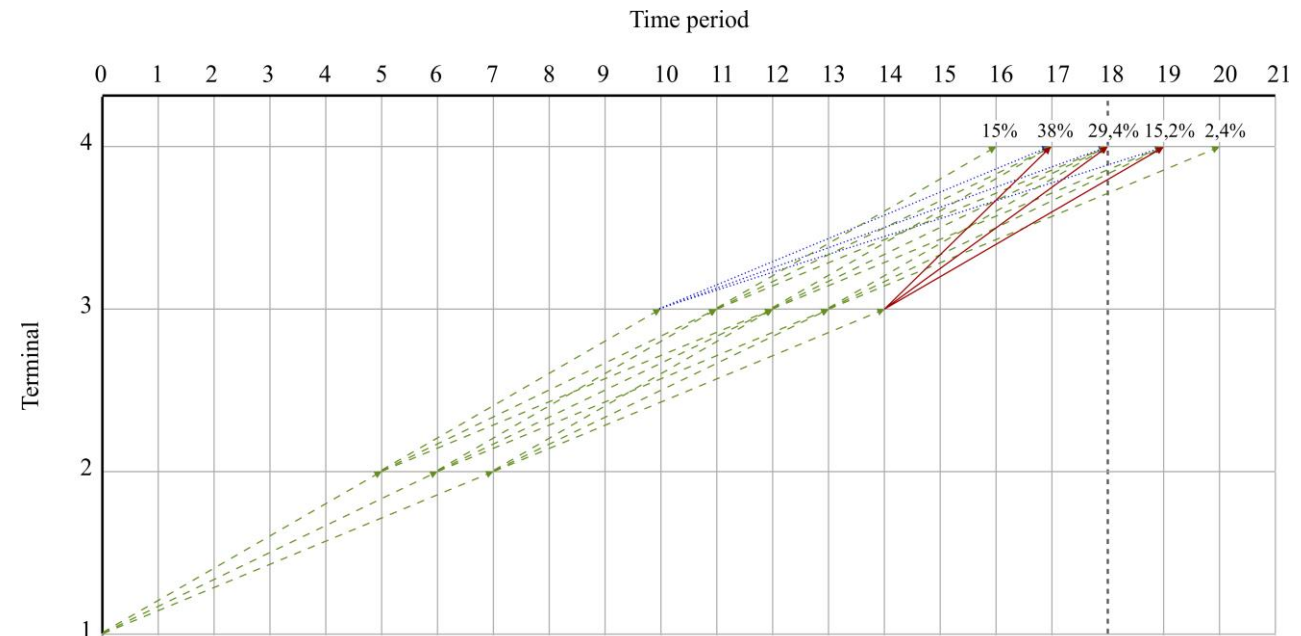
Output of the model



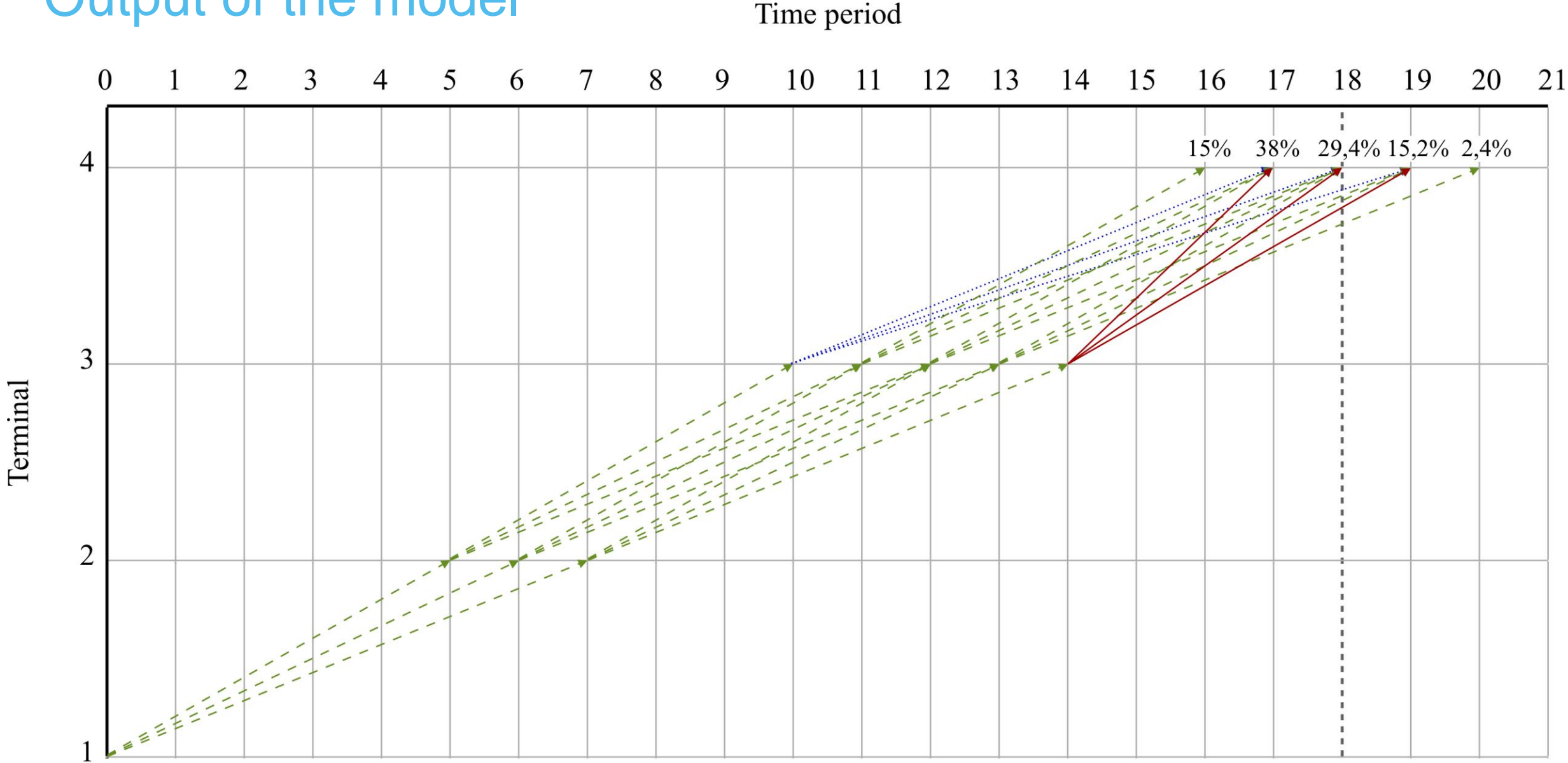
Output

- Decision guide conditional on the transit time outcome

- Which decision to take in a terminal, given the time period in which the decision is to be made



Output of the model

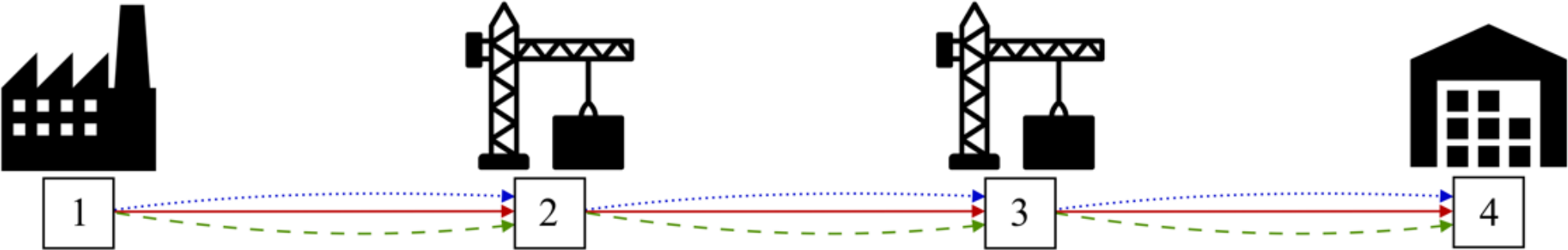


Numerical study

Origin terminal

Intermediate terminals

Destination terminal



Numerical study - Performance analysis.

Common practice

One mode Multiple modes Real-time information

▪ Unimodal road transportation

x

▪ Unimodal rail transportation

x

▪ Unimodal barge transportation

x

▪ Multimodal transportation

x

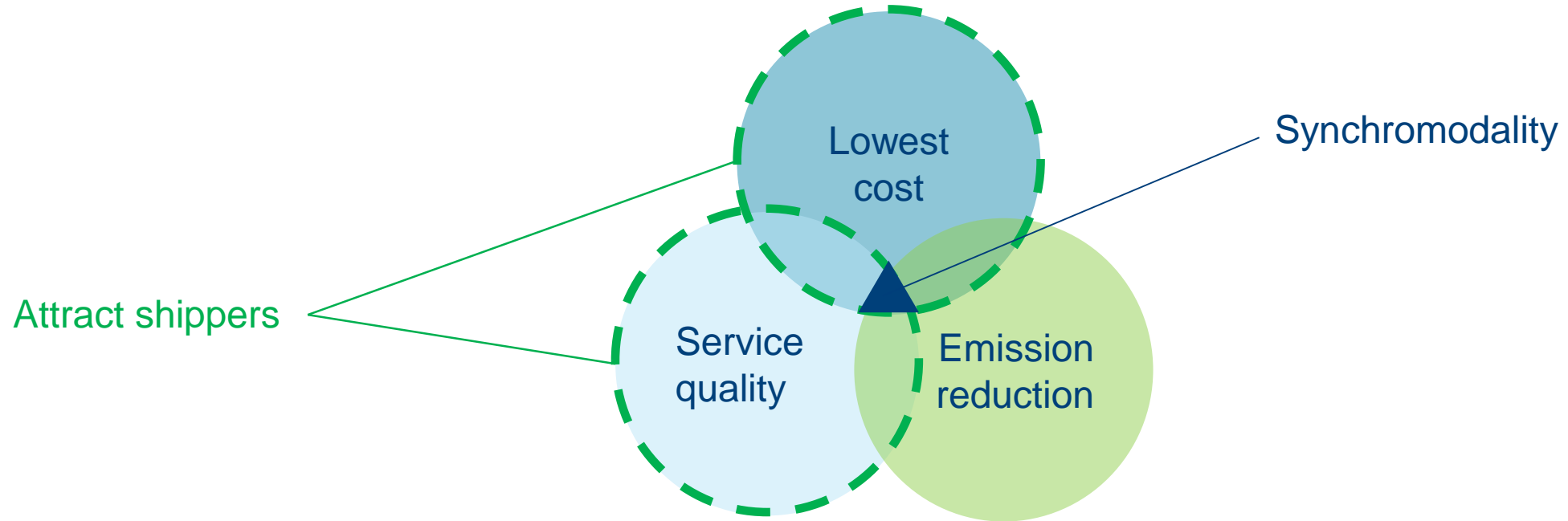
▪ Synchromodal transportation

x

x

Value of real-time planning

Synchromodality performs well in terms of cost, service quality and environmental impact.



- Synchromodality offers a combination of advantages that allows to achieve sustainable freight transportation services at a favorable price and service quality.

Numerical study – Sensitivity analyses.



Penalty per period
of late delivery



Transshipment cost
in terminals



Carbon tax
per ton CO₂



Reliability of
transportation modes

Numerical study – Sensitivity analyses.



Penalty per period
of late delivery



Transshipment cost
in terminals

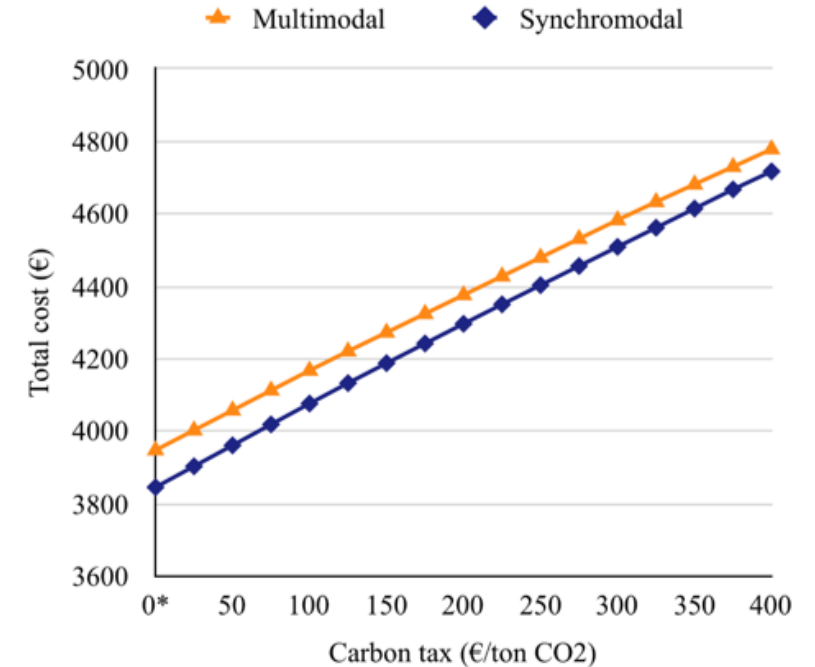
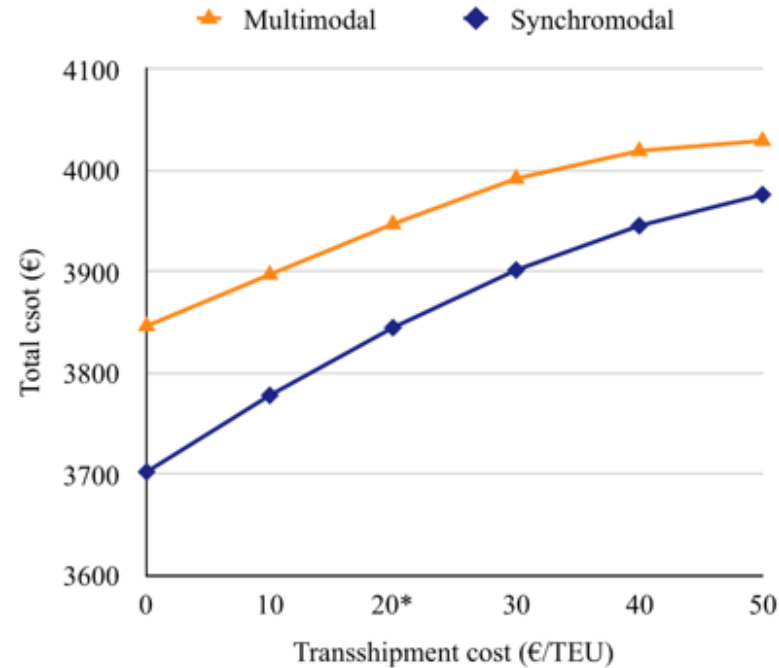
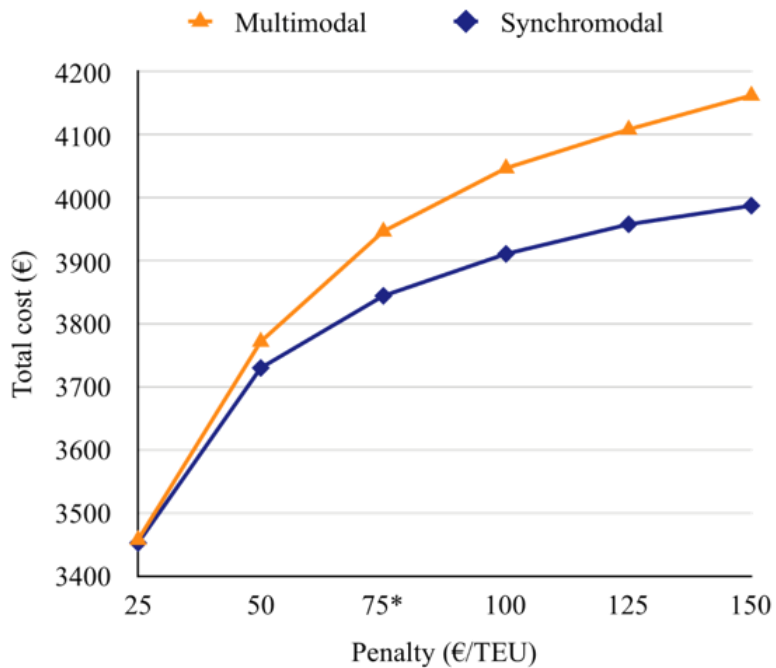


Carbon tax
per ton CO₂



Reliability of
transportation modes

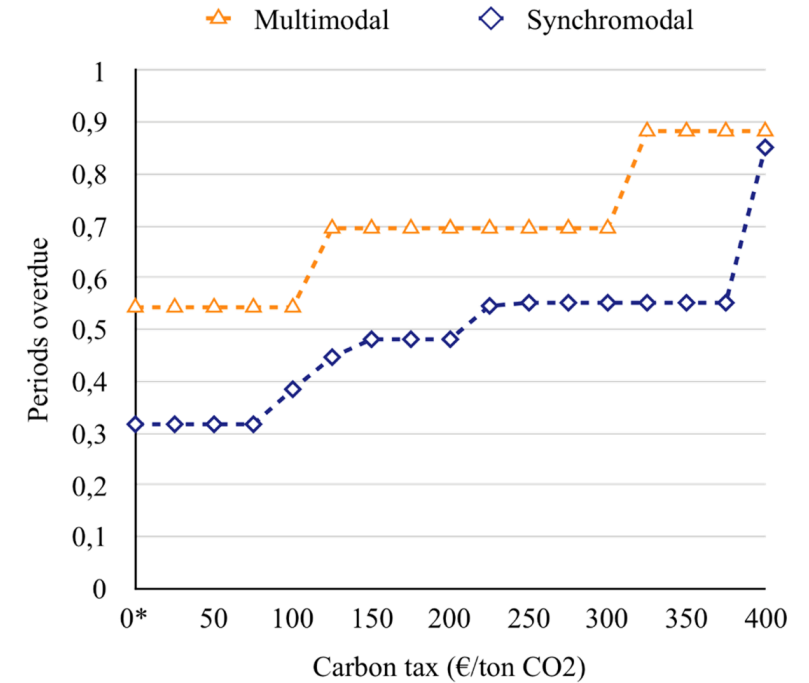
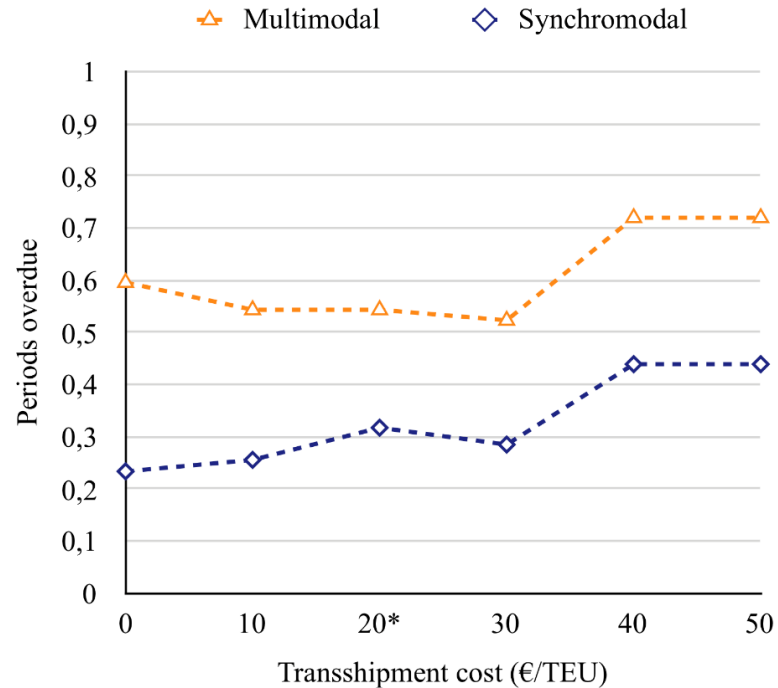
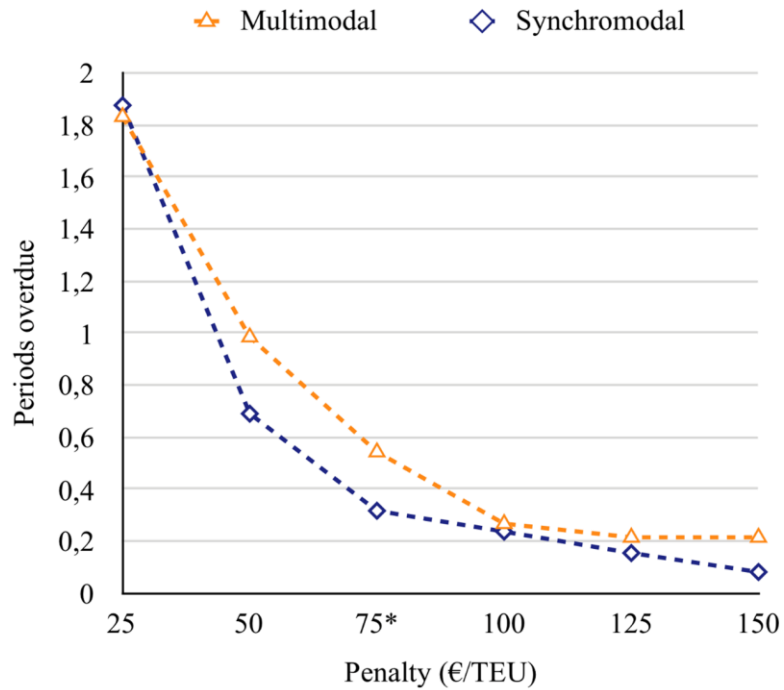
Numerical study – Impact of changing cost parameters.



Synchronomodality > Multimodality

- Cost
 - Service quality
- regardless of the parameter value

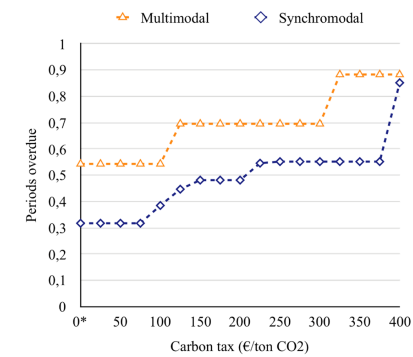
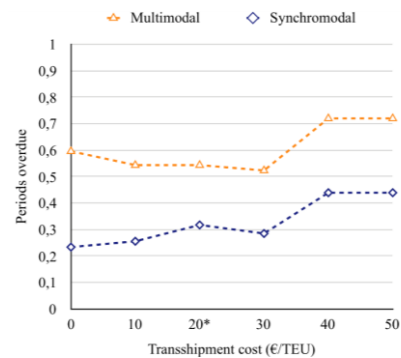
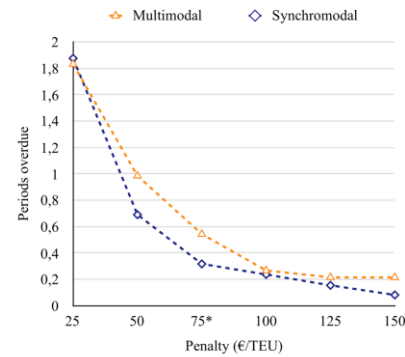
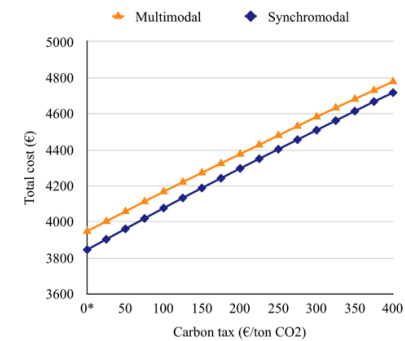
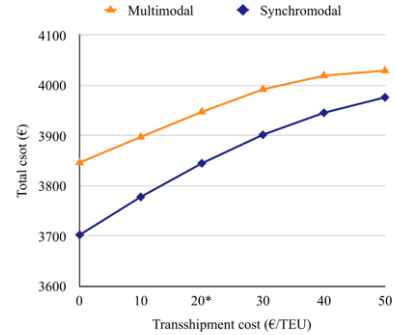
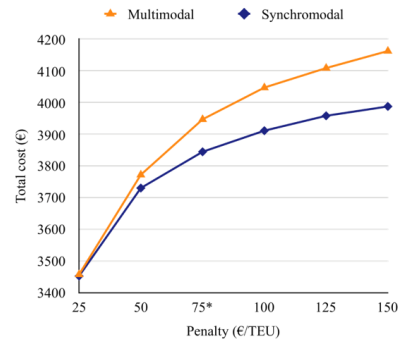
Numerical study – Impact of changing cost parameters.



Synchronodality > Multimodality

- Cost
 - Service quality
- regardless of the parameter value

Numerical study – Impact of changing cost parameters.



Synchronomodality > Multimodality ➤ Value of real-time information

- Cost
 - Service quality
- regardless of the parameter value

Numerical study – Impact of carbon tax.



Penalty per period
of late delivery



Transshipment cost
in terminals

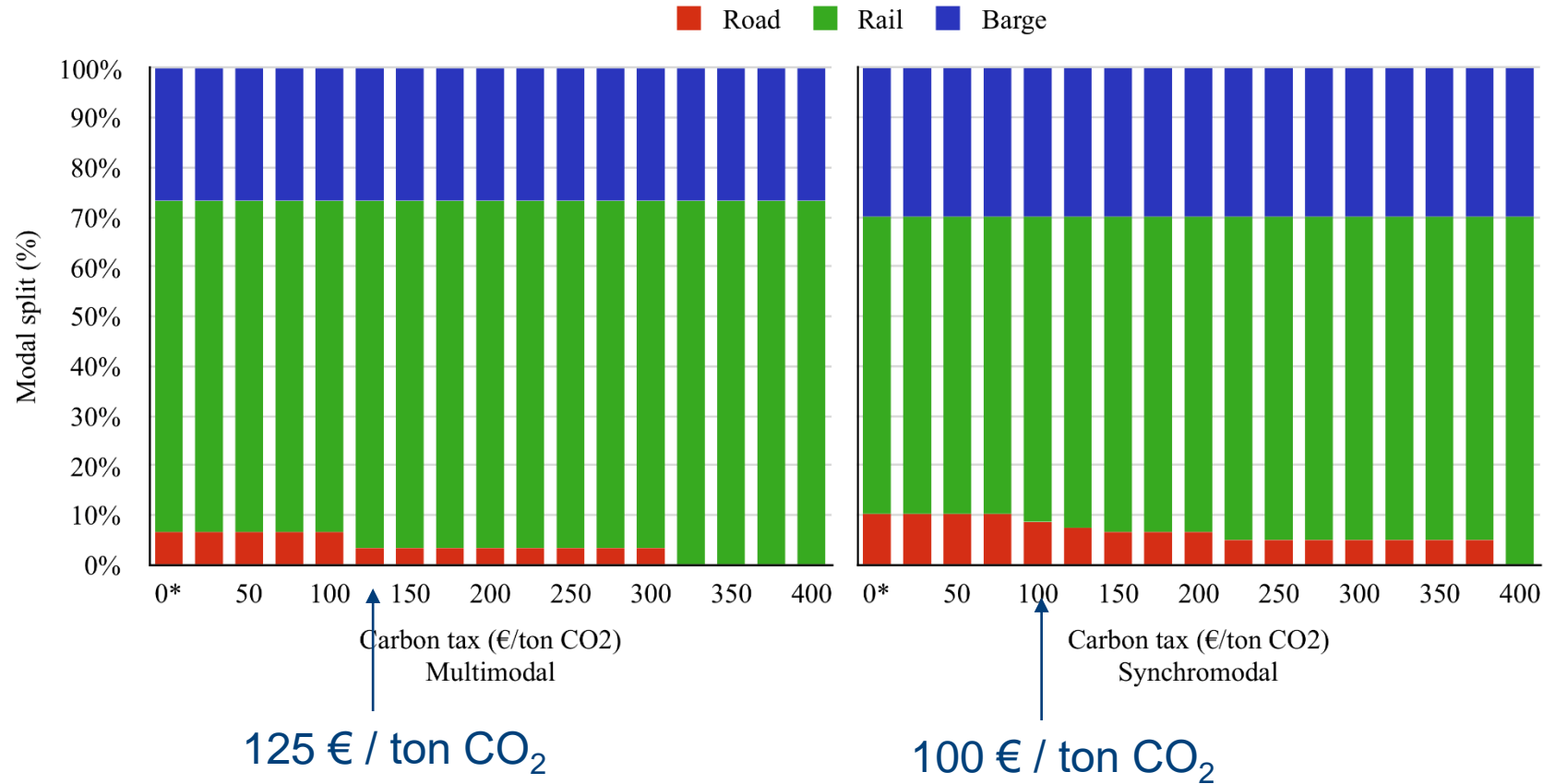
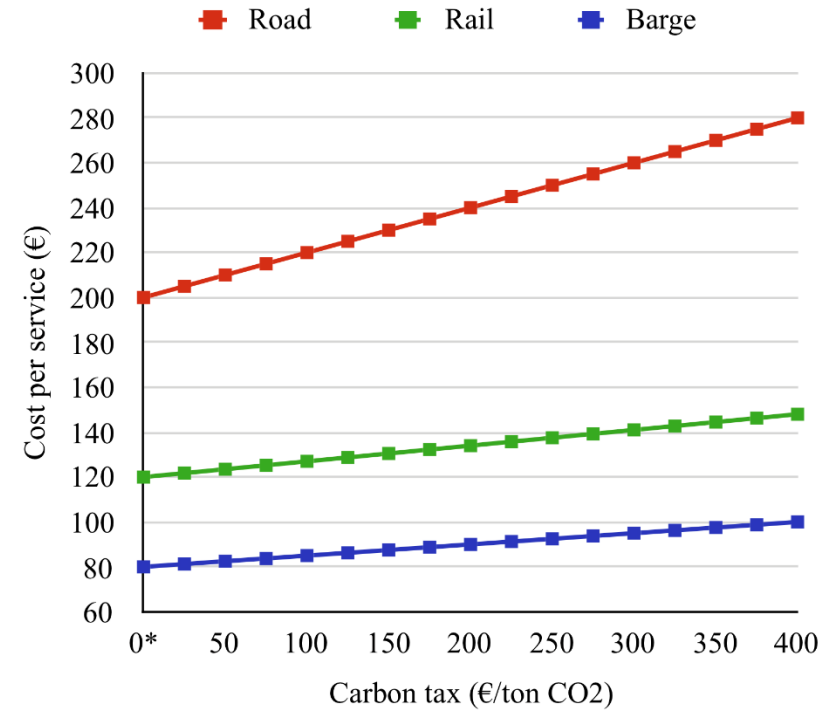


Carbon tax
per ton CO₂



Reliability of
transportation modes

Numerical study – Impact of carbon tax.



125 € / ton CO₂

100 € / ton CO₂

Numerical study – Impact of reliability.



Penalty per period
of late delivery



Transshipment cost
in terminals

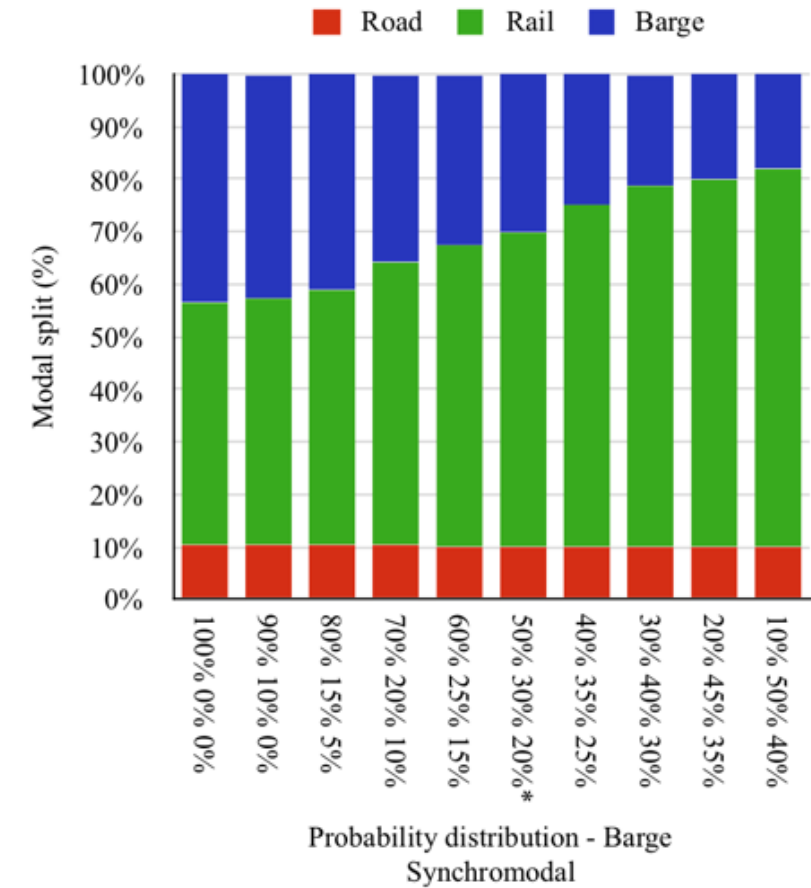
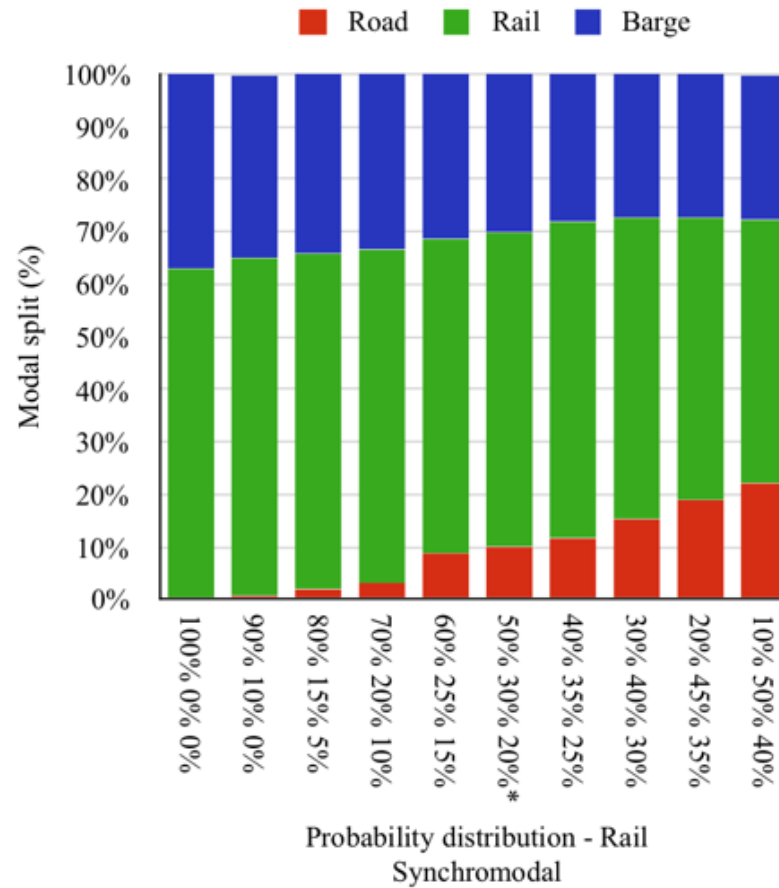
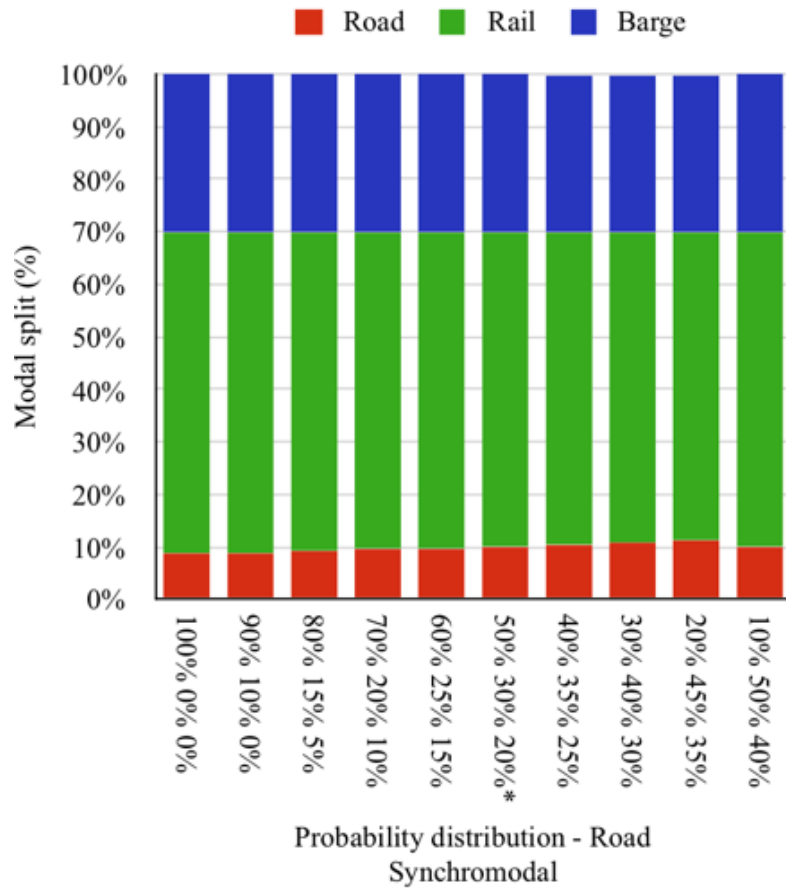


Carbon tax
per ton CO₂



Reliability of
transportation modes

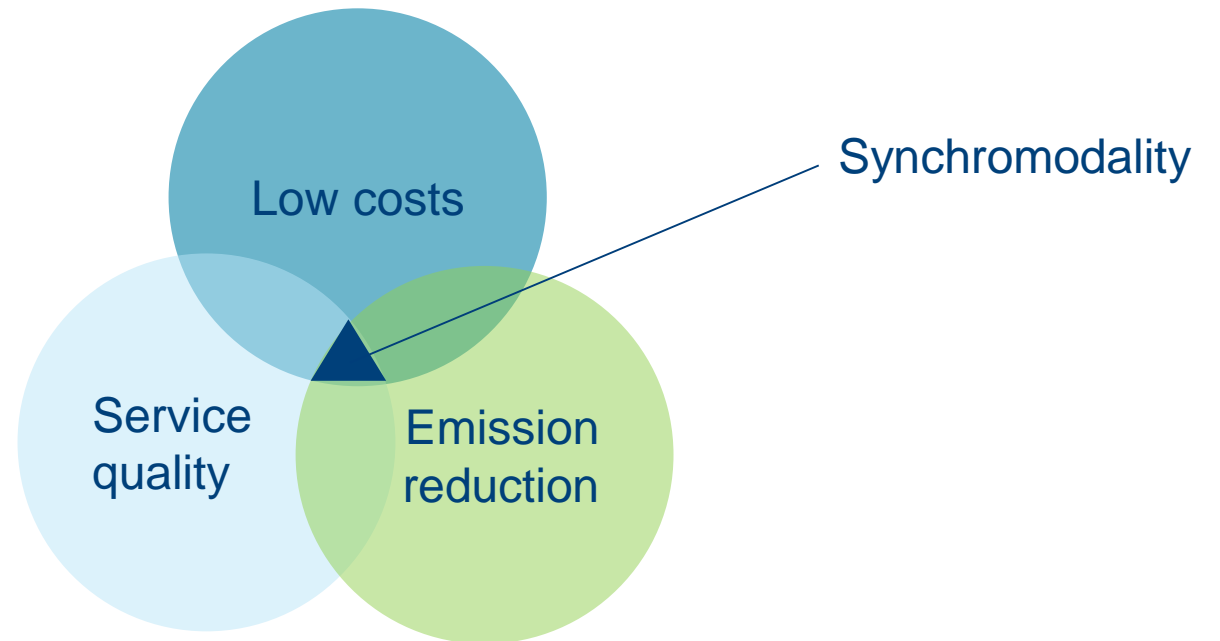
Numerical study – Impact of reliability.



Conclusion

We developed a synchromodal planning model to construct optimal transportation routes in a multimodal network with stochastic transit times.

Synchromodality offers a combination of advantages that allows to achieve sustainable freight transportation services at a favorable price and service quality.





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Additional information

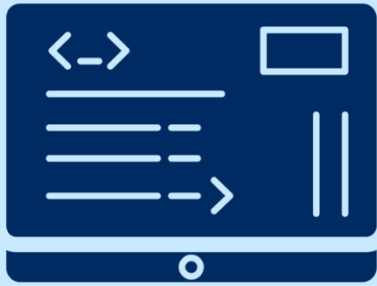




Methodology

Objective function

The model minimizes total cost.



Optimization model

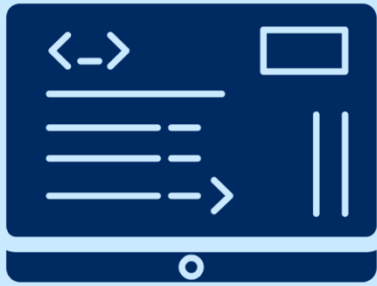
- Construct optimal transportation routes
- MILP

Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

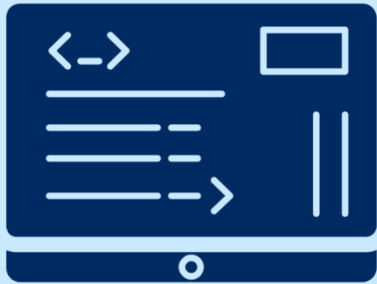
Objective function

Minimize

$$\underbrace{\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n}_{\text{variable leg transportation cost}} + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

variable leg
transportation cost

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

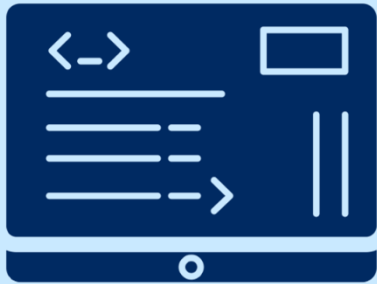
Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \underbrace{\sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n}_{\text{terminal transshipment cost}} + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

terminal
transshipment cost

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

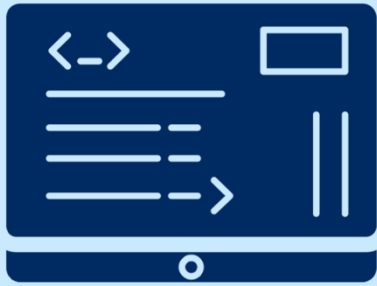
Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \underbrace{\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n}_{\text{overdue penalty cost}}$$

overdue
penalty cost

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

Objective function

Minimize

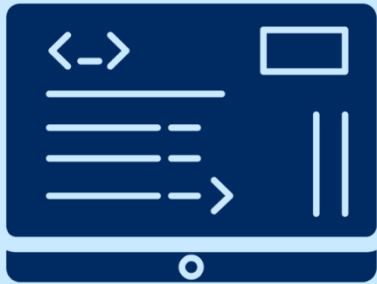
$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

variable leg
transportation cost

terminal
transshipment cost

overdue
penalty cost

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

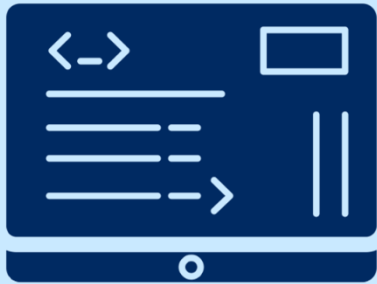
variable leg
transportation cost

terminal
transshipment cost

overdue
penalty cost

low cost

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

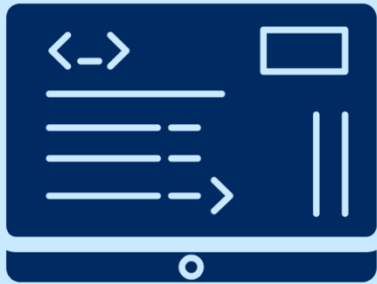
variable leg
transportation cost

terminal
transshipment cost

overdue
penalty cost

on-time delivery

The model minimizes total cost.



Optimization model

- Construct optimal transportation routes
- MILP

Objective function

Minimize

$$\sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[C^V]_{i,j,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{g,m \in \mathcal{M}} E[C^T]_{i,g,m,0}^n + \sum_{n \in \mathcal{O}} \sum_{(i,j,m) \in \mathcal{A}} E[\rho]_{i,j,m,0}^n$$

variable leg
transportation cost

terminal
transshipment cost

overdue
penalty cost

low cost

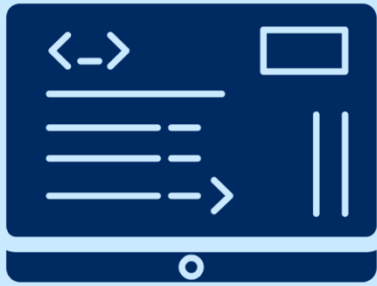
on-time delivery



Methodology

Constraints

Subjected to three constraint sets.



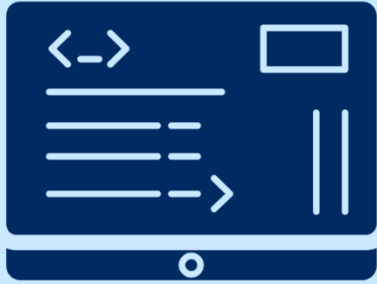
Optimization model

- Construct optimal transportation routes
- MILP

Constraints

- Network flow constraints
- Expected cost constraints
- Expected penalty constraints

Methodology



Optimization model

Constraints

Network flow constraints

$$\sum_{(o_n,j,m) \in \mathcal{A}} x_{o_n,j,m,0}^n = 1$$

$$\forall n \in \mathcal{O}$$

$$\sum_{(i,j,m) \in \mathcal{A}} x_{i,j,m,0}^n = 1$$

$$\forall n \in \mathcal{O}$$

$$x_{i,j,m,t}^n \leq \sum_{(j,k,h) \in \mathcal{A}} x_{j,k,h,t+l_{i,j,m}^s}$$

$$\forall n \in \mathcal{O}, \forall (i,j,m) \in \mathcal{A}, \forall t \in \mathcal{T}, \forall s \in \mathcal{S}$$

$$\sum_{(i,j,m) \in \mathcal{A}} x_{i,j,m,t}^n \leq 1$$

$$\forall n \in \mathcal{O}, \forall i \in \mathcal{N}, \forall t \in \mathcal{T}$$

$$x_{d_n,d_n,storage,T}^n = 1$$

$$\forall n \in \mathcal{O}$$

$$\sum_{(i,j,m) \in \mathcal{A}} x_{i,j,m,T}^n = 1$$

$$\forall n \in \mathcal{O}$$

$$1 + w_{i,g,m,t+l_{k,i,g}^s}^n \geq x_{k,i,g,t}^n + x_{i,j,m,t+l_{k,i,g}^s}^n$$

$$\forall (k,i,g) \in \mathcal{A}, \forall (i,j,m) \in \mathcal{A}, \forall t \in \mathcal{T}, \forall s \in \mathcal{S}$$

$$w_{i,storage,m,0}^n \geq x_{i,j,m,0}^n$$

$$\forall (i,j,m) \in \mathcal{A}, i \in \mathcal{N}_o$$

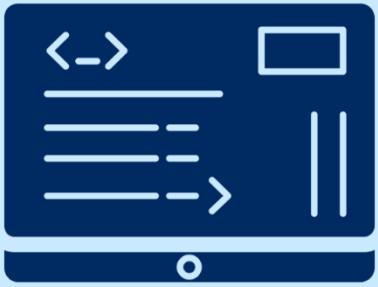
$$x_{i,j,m,t}^n \in \{0,1\}$$

$$\forall n \in \mathcal{O}, \forall (i,j,m) \in \mathcal{A}, \forall t \in \mathcal{T}$$

$$w_{i,g,m,t}^n \in \{0,1\}$$

$$\forall n \in \mathcal{O}, \forall i \in \mathcal{N}, \forall g, m \in \mathcal{M}, \forall t \in \mathcal{T}$$

Methodology



Optimization model

Constraints

Expected cost constraints

$$E[C^V]_{i,j,m,t}^n \geq c_{i,j,m}^V f_n + \sum_s p_{i,j,m}^s \sum_{(j,k,h) \in \mathcal{A}} E[C^V]_{i,j,m,t+l_{i,j,m}^s}^n - Z(1 - x_{i,j,m,t}^n)$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, \forall t \in \mathcal{T}$$

$$E[C^V]_{i,j,m,t}^n \geq 0$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, \forall t \in \mathcal{T}$$

$$E[C^T]_{i,g,m,t}^n \geq c_{g,m}^T f_n + \sum_s p_{i,j,m}^s \sum_{(j,k,h) \in \mathcal{A}} E[C^T]_{i,m,h,t+l_{i,j,m}^s}^n - Z(1 - w_{i,g,m,t}^n) - Z(1 - x_{i,j,m,t}^n)$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, i \in \mathcal{N}_t, \forall g \in \mathcal{M}, \forall t \in \mathcal{T}$$

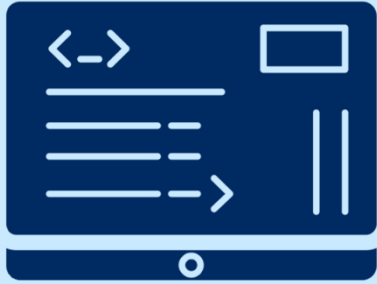
$$E[C^T]_{i,g,m,t}^n \geq \sum_s p_{i,j,m}^s \sum_{(j,k,h) \in \mathcal{A}} E[C^T]_{i,m,h,t+l_{i,j,m}^s}^n - Z(1 - w_{i,g,m,t}^n) - Z(1 - x_{i,j,m,t}^n)$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, i \in \mathcal{N}_o, \forall g \in \mathcal{M}, \forall t \in \mathcal{T}$$

$$E[C^T]_{i,g,m,t}^n \geq 0$$

$$\forall n \in \mathcal{O}, \forall i \in \mathcal{N}, \forall g, m \in \mathcal{M}, \forall t \in \mathcal{T}$$

Methodology



Optimization model

Constraints

Expected penalty
constraints

$$E[\rho]_{i,j,m,t}^n \geq \sum_s p_{i,j,m}^s \sum_{(j,k,h) \in \mathcal{A}} E[\rho]_{j,k,h,t+l_{i,j,m}^s}^n - Z(1-x_{i,j,m,t}^n)$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, i \in \mathcal{N}_0 \cup \mathcal{N}_t, \forall t \in \mathcal{T}$$

$$E[\rho]_{i,j,m,t}^n \geq (t - k_n) f_n \rho - Z(1-x_{i,j,m,t}^n)$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, i \in \mathcal{N}_d, \forall t \in \mathcal{T}$$

$$E[\rho]_{i,j,m,t}^n \geq 0$$

$$\forall n \in \mathcal{O}, \forall (i, j, m) \in \mathcal{A}, \forall t \in \mathcal{T}$$



Numerical study

Sensitivity analyses

Numerical study – Impact of penalty cost



Penalty per period
of late delivery



Transshipment cost
in terminals

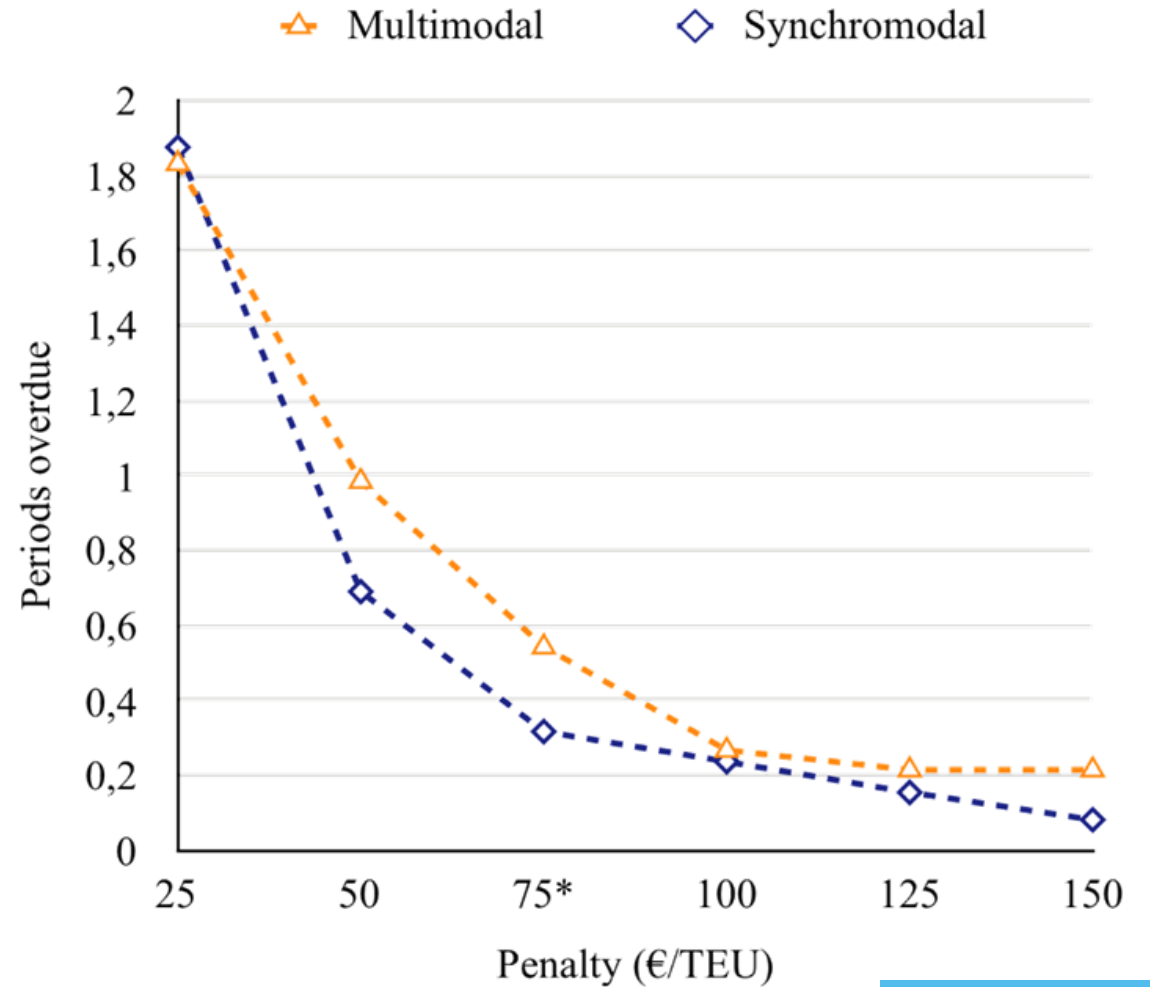
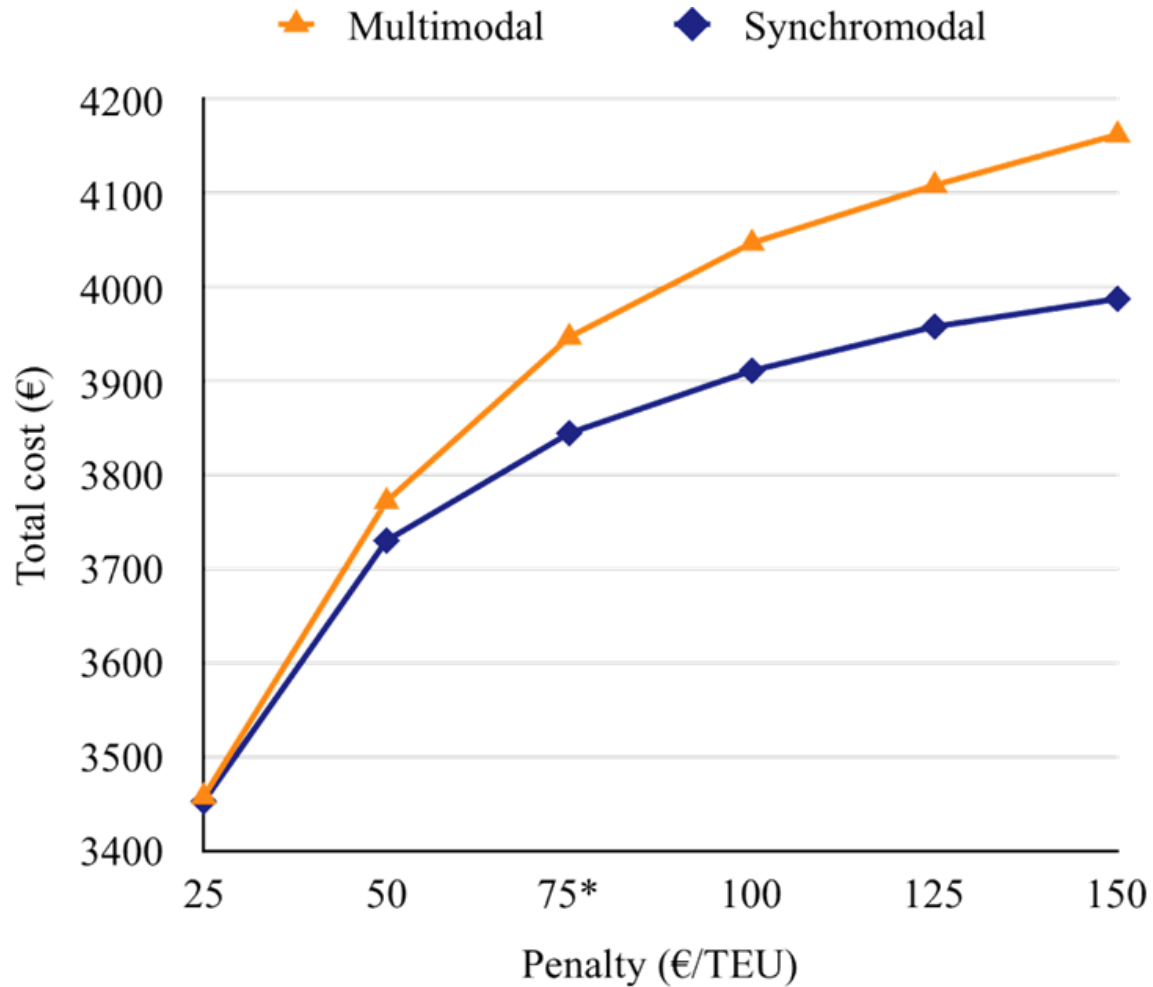


Carbon tax
per ton CO₂



Reliability of
transportation modes

Numerical study – Impact of penalty cost



Numerical study – Impact of transshipment cost



Penalty per period
of late delivery



Transshipment cost
in terminals

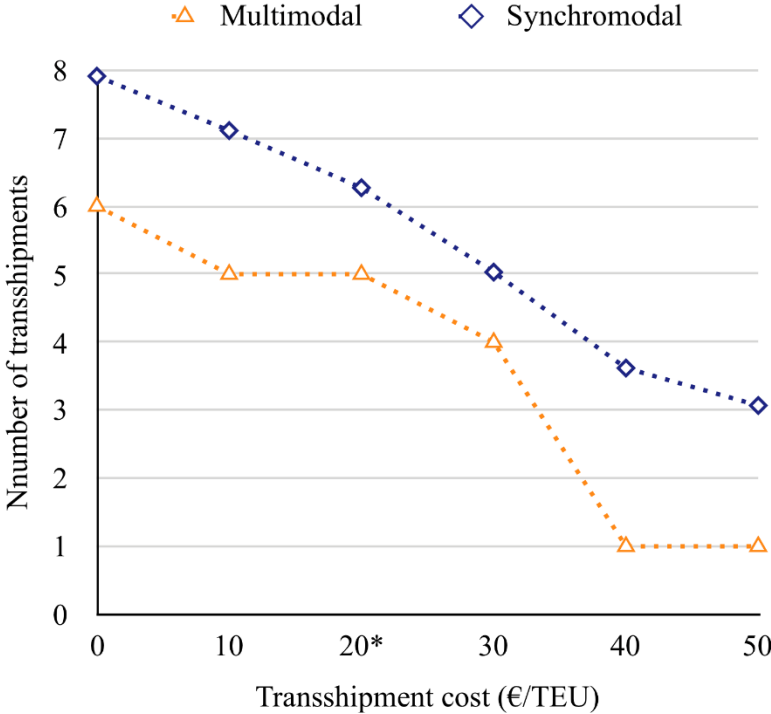
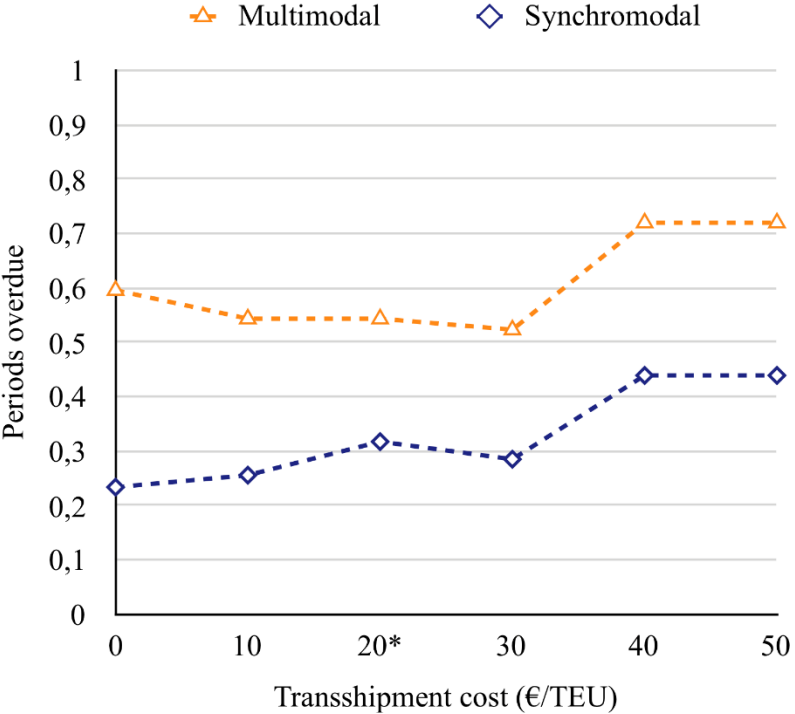
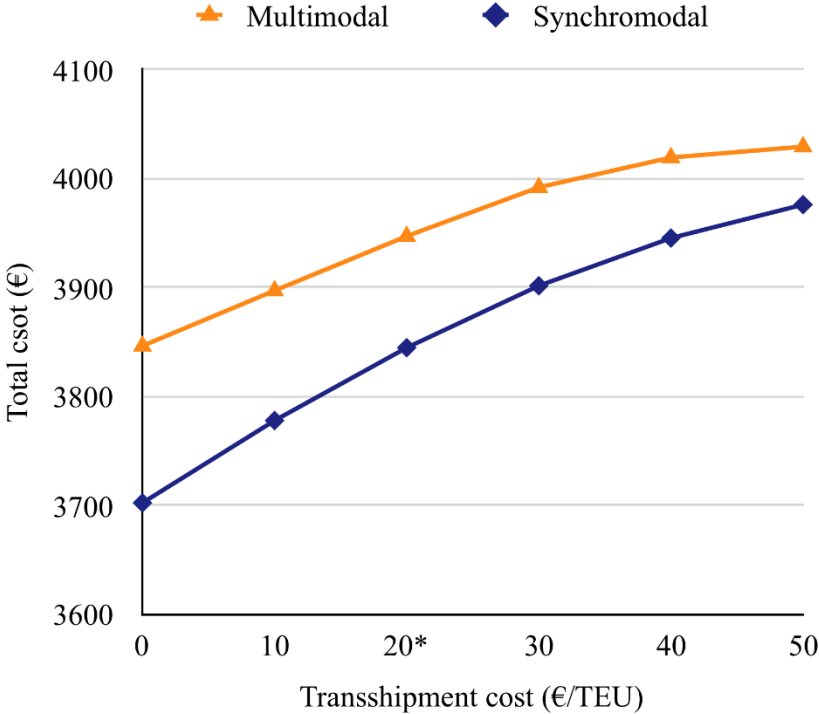


Carbon tax
per ton CO₂



Reliability of
transportation modes

Numerical study – Impact of transshipment cost



Numerical study – Sensitivity analyses



Penalty per period
of late delivery



Transshipment cost
in terminals



Carbon tax
per ton CO₂



Probability distribution
over scenarios

Synchromodality > Multimodality

- Cost
 - Service quality
- regardless of the parameter value

Relative cost reduction ↑ :

- Penalty ↑
- Transshipment cost ↓

Numerical study – Impact of carbon tax



Penalty per period
of late delivery



Transshipment cost
in terminals

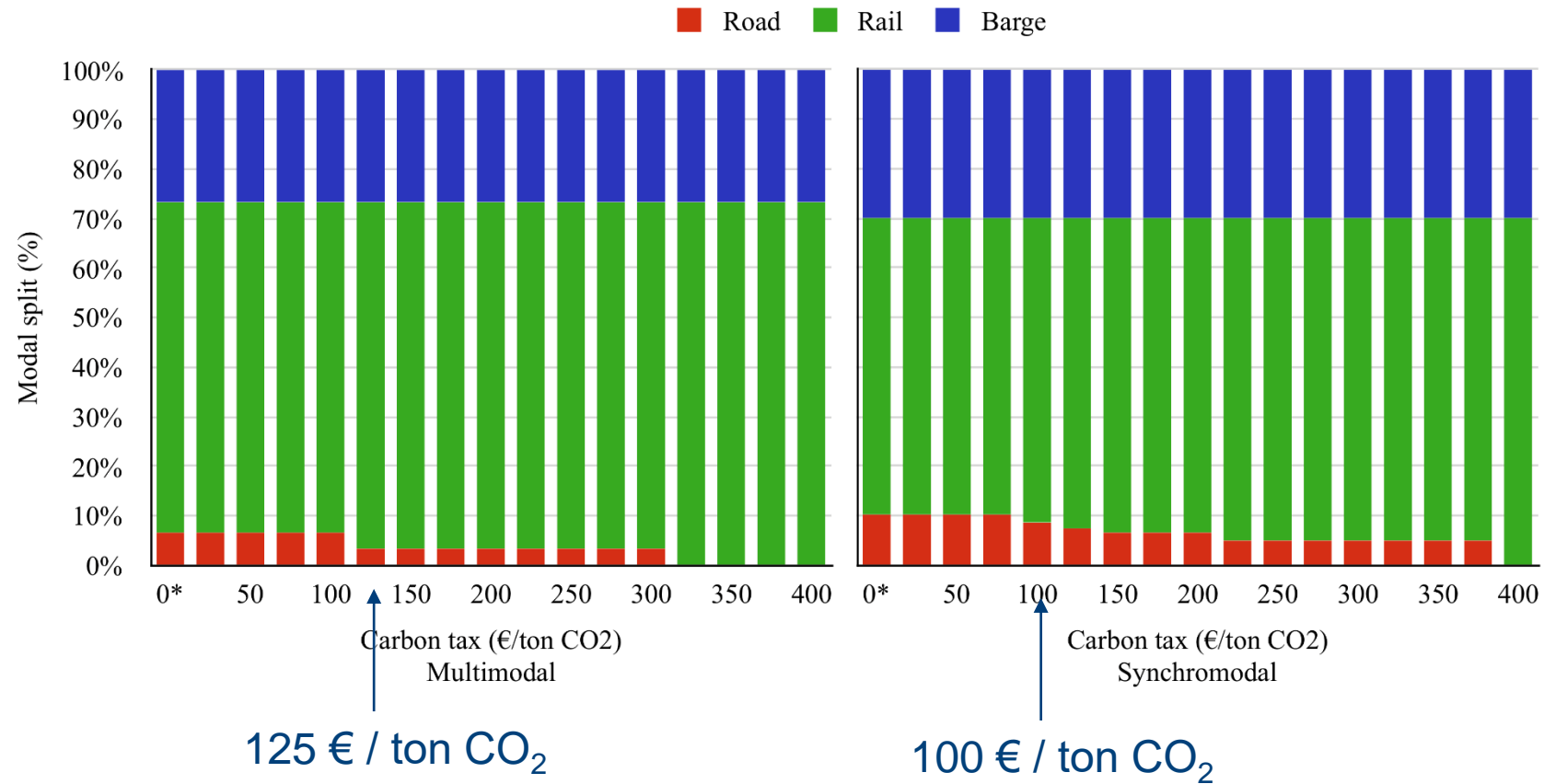
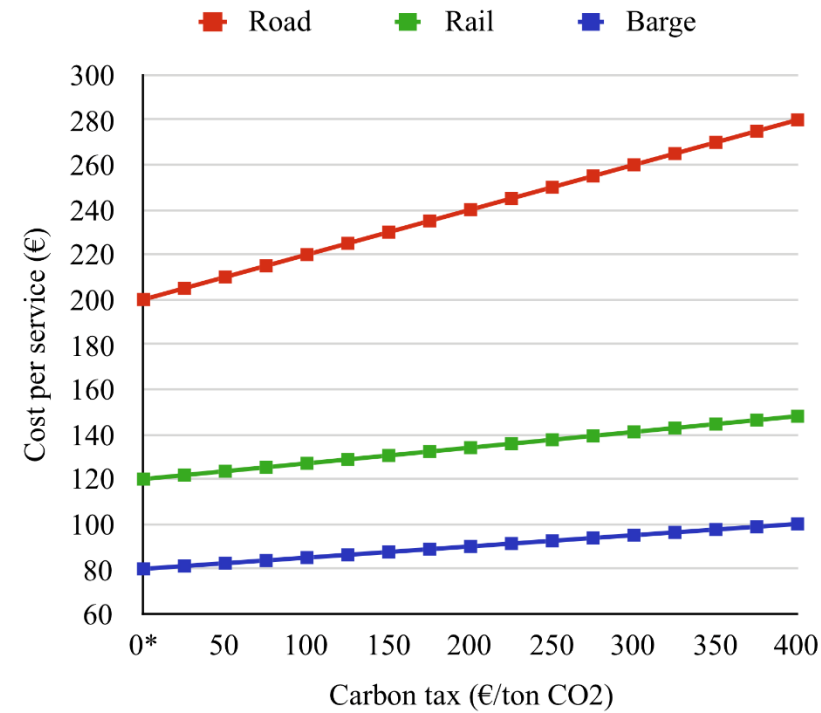


Carbon tax
per ton CO₂



Reliability of
transportation modes

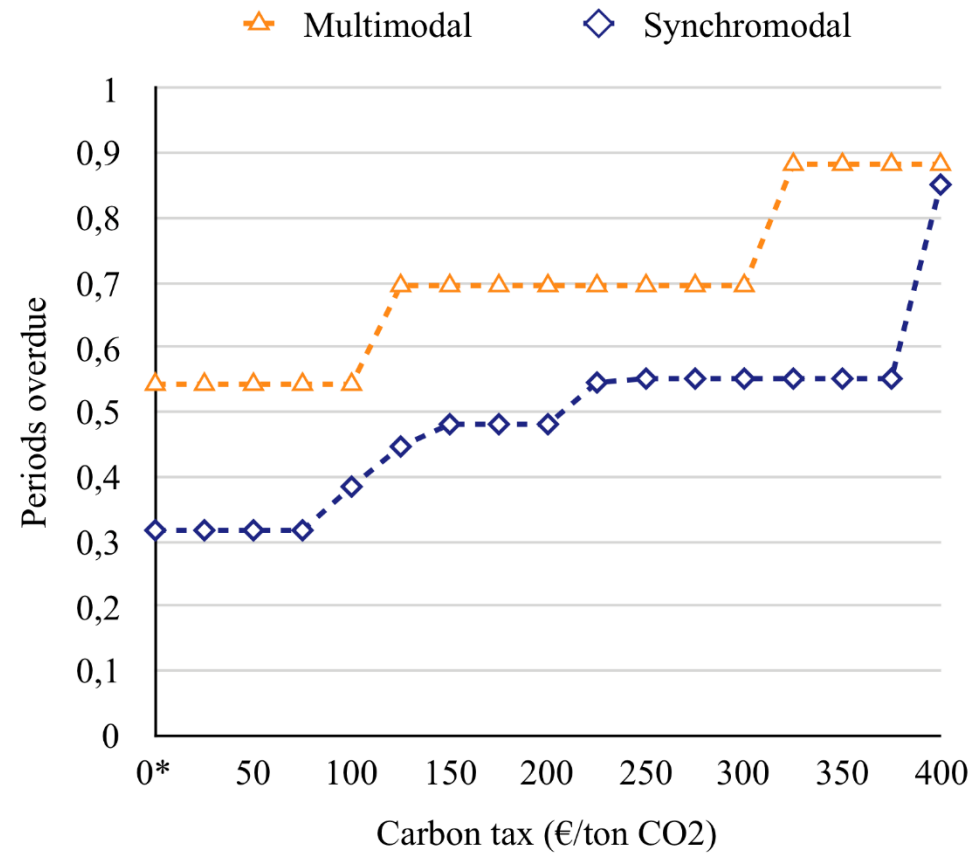
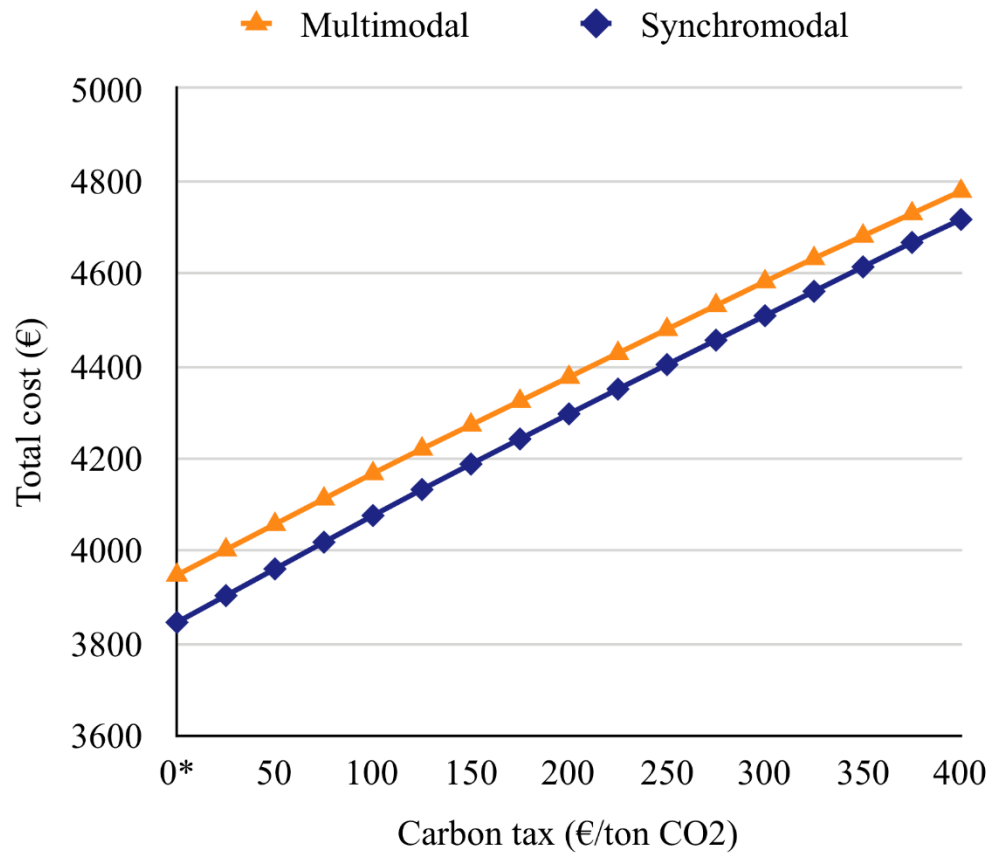
Numerical study – Impact of carbon tax



125 € / ton CO₂

100 € / ton CO₂

Numerical study – Impact of carbon tax



Numerical study – Impact of reliability



Penalty per period
of late delivery



Transshipment cost
in terminals

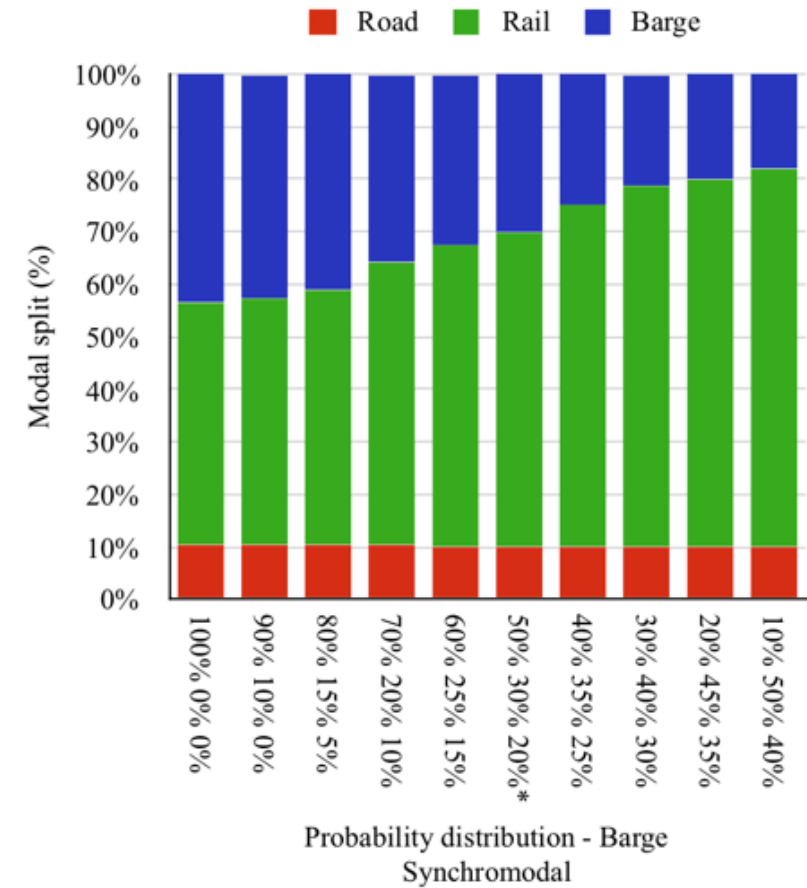
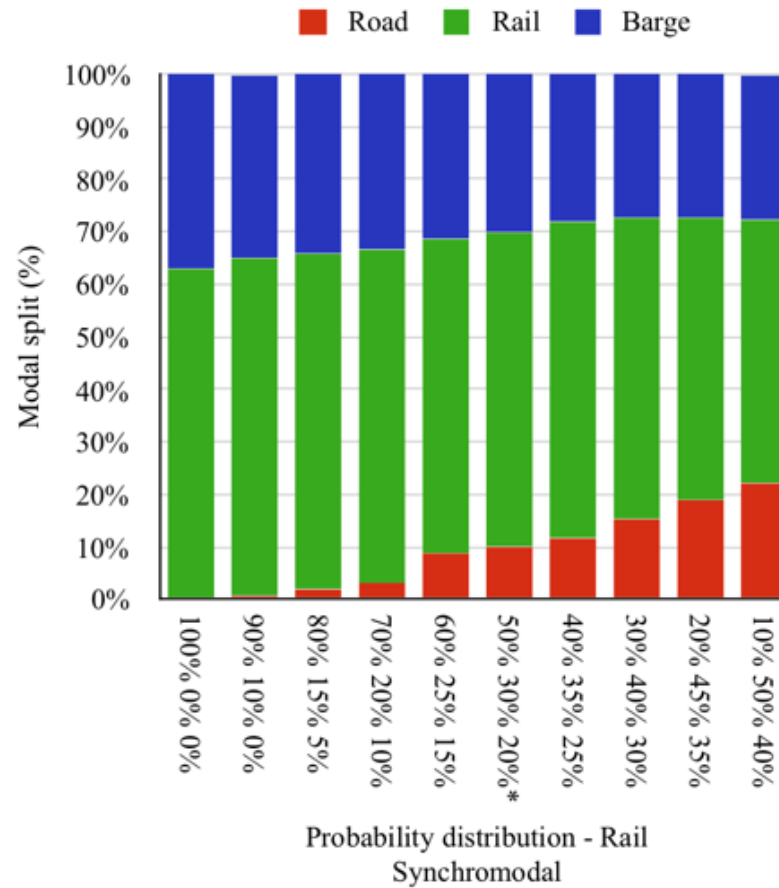
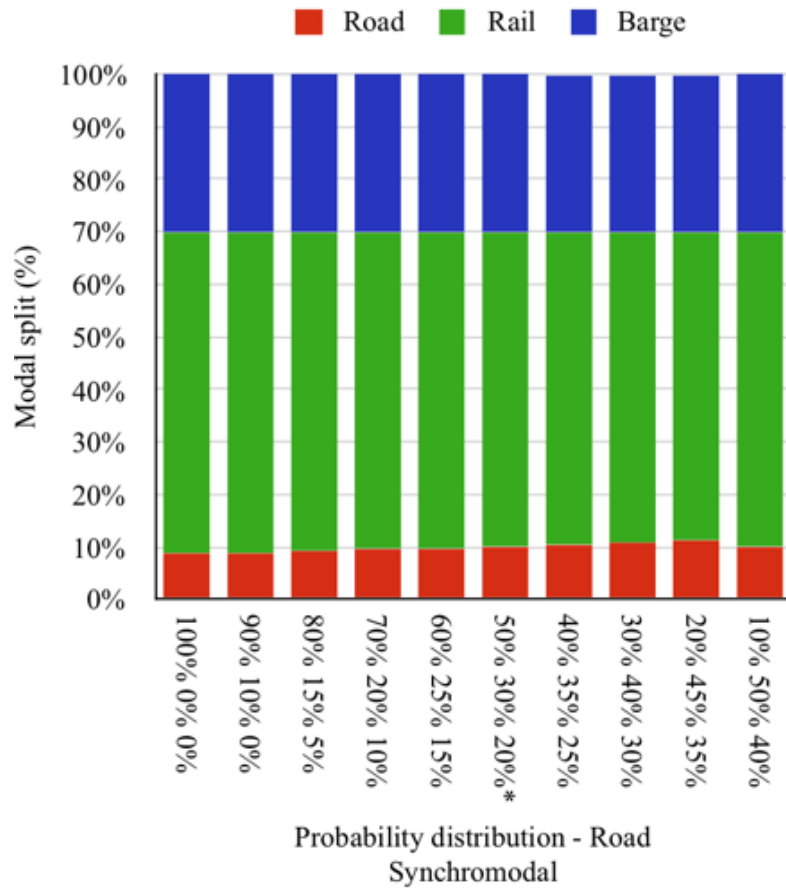


Carbon tax
per ton CO₂

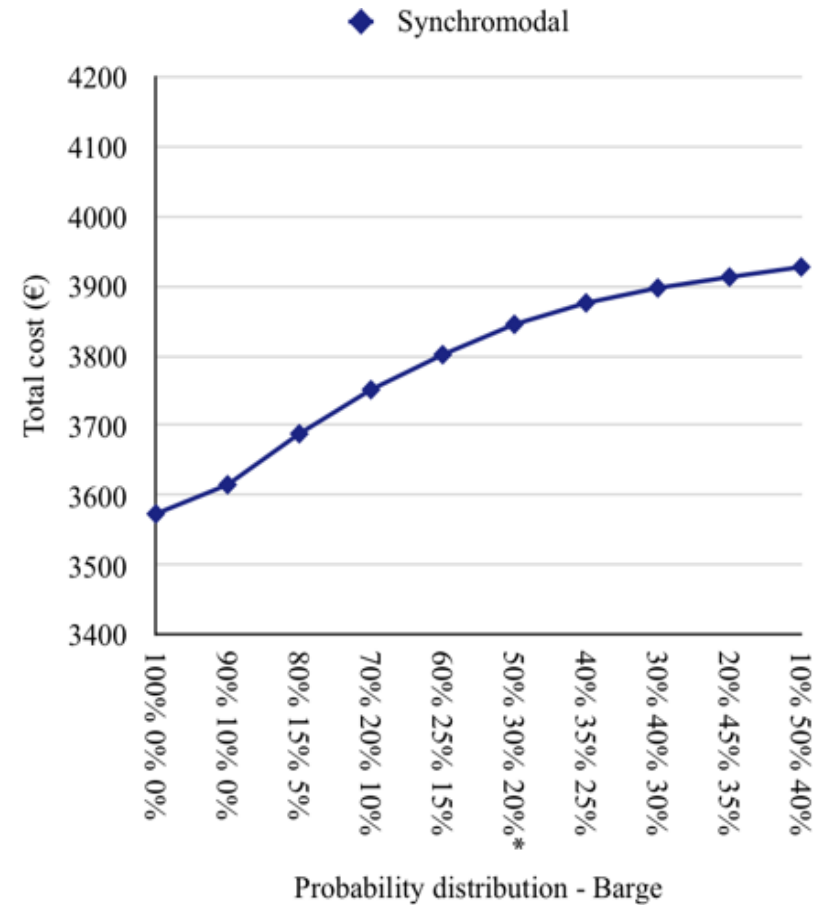
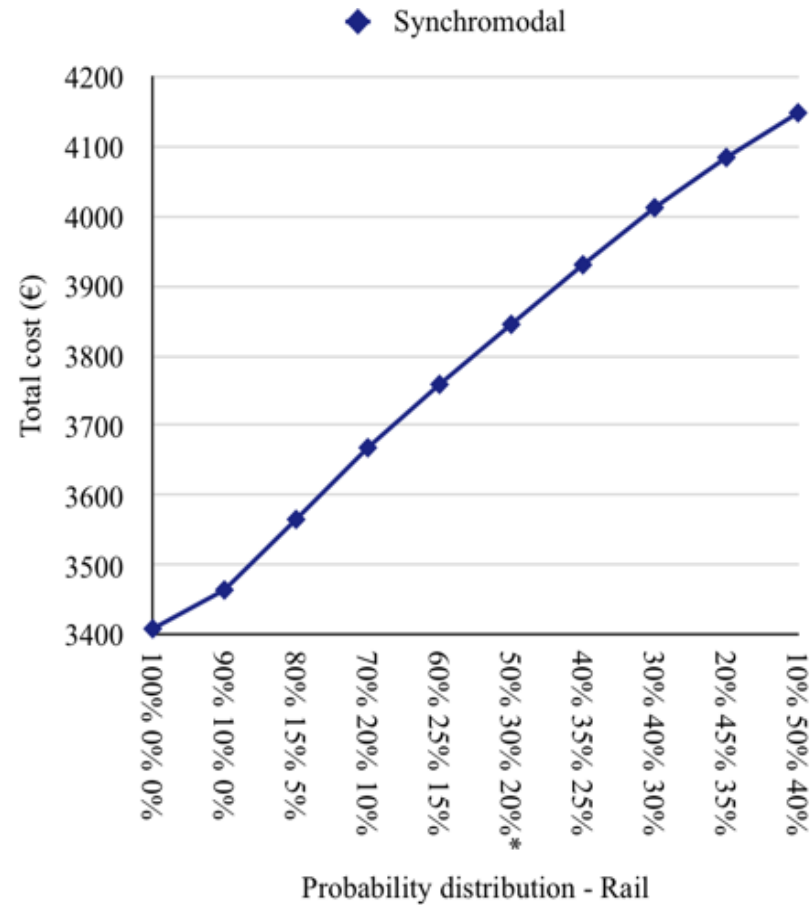
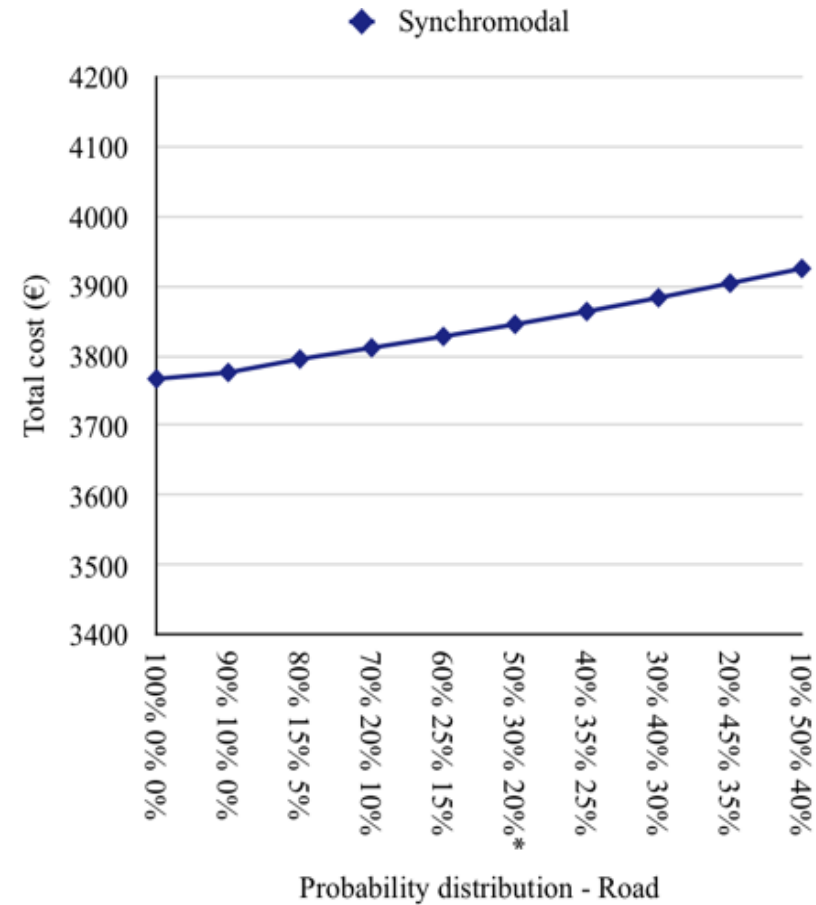


Reliability of
transportation modes

Numerical study – Impact of reliability



Numerical study – Impact of reliability



Numerical study – Impact of reliability

